

1. $\cot \theta = 4$

$\cot^2 \theta + 1 = \csc^2 \theta$

$(4)^2 + 1 = \csc^2 \theta$

$16 + 1 = \csc^2 \theta$

$\csc \theta = \sqrt{17}$

$\sin \theta = \frac{1}{\sqrt{17}} = \frac{\sqrt{17}}{17}$

~~$\cot^2 \theta + 1 = \sec^2 \theta$~~

$(\frac{1}{4})^2 + 1 = \sec^2 \theta$

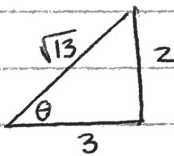
$\frac{1}{16} + 1 = \sec^2 \theta$

$\frac{17}{16} = \sec^2 \theta$

$\frac{\sqrt{17}}{4} = \sec \theta$

$\frac{4}{\sqrt{17}} = \frac{4\sqrt{17}}{17} = \cos \theta$

2. $\tan \theta = -\frac{2}{3}$



$2^2 + 3^2 = c^2$

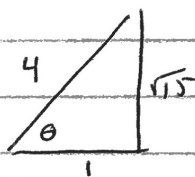
$13 = c^2$

$c = \sqrt{13}$

~~$\sec \theta = \frac{3}{\sqrt{13}}$~~

$\sec \theta = -\frac{\sqrt{13}}{3}$

3. $\cos \theta = \frac{1}{4}$



$1^2 + b^2 = 4^2$

$b^2 = 15$

$b = \sqrt{15}$

$\tan \theta = \sqrt{15}$

$\csc \theta = \frac{4}{\sqrt{15}} = \frac{4\sqrt{15}}{15}$

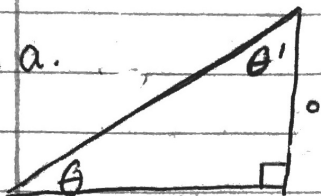
4. $\frac{\sin(-x)}{\tan(-x)} = \frac{-\sin x}{-\tan x} = \frac{\sin x}{\frac{\sin x}{\cos x}} = \sin x \cdot \frac{\cos x}{\sin x} = \cos x$

5. $\frac{\sec^2 x}{\cot^2 x + 1} = \frac{\sec^2 x}{\csc^2 x} = \frac{\frac{1}{\cos^2 x}}{\frac{1}{\sin^2 x}} = \frac{1}{\cos^2 x} \cdot \frac{\sin^2 x}{1} = \tan^2 x$

6. $\frac{\sin(90-x)}{\cot^2(90-x) + 1} = \frac{\sin(90-x)}{\csc^2(90-x)} = \frac{\cos(x)}{\sec^2(x)} = \frac{\cos x}{\frac{1}{\cos^2 x}} = \cos x \cdot \cos^2 x = \cos^3 x$

7. $\frac{\sin x}{1 + \sec x} \cdot \frac{(1 - \sec x)}{(1 - \sec x)} = \frac{\sin x - \sin x \sec x}{1 - \sec^2 x} = \frac{\sin x - \sin x \sec x}{-\tan^2 x} = \frac{\sin x}{-\tan^2 x} = \frac{\sin x}{-\tan^2 x} \cdot \frac{\cos x}{\cos x} = \frac{\sin x \cos x}{-\frac{\sin^2 x}{\cos^2 x}} = \frac{\sin x \cos x}{-\frac{\sin^2 x}{\cos^2 x}} = -\cot x \cos x + \cot x$

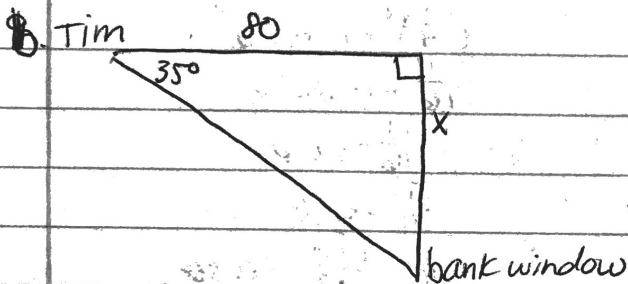
8. a.



$$\theta' = 180 - 90 - \theta$$

$$\theta' = 90 - \theta$$

$$\begin{aligned} \cos \theta' &= \cos(90 - \theta) \\ &= \sin(\theta) \end{aligned}$$



$$\tan 35 = \frac{x}{80}$$

$$x = 56 \text{ ft}$$

9. D. $\frac{1}{\sin(90-\theta)} = \frac{1}{\cos \theta} = \sec \theta$

10. $\frac{\cos \theta}{1 + \sin \theta} - \frac{\cos \theta}{1 - \sin \theta} = -2 \tan \theta$

$$\frac{(1 - \sin \theta) \cos \theta}{1 - \sin^2 \theta} - \frac{(1 + \sin \theta) \cos \theta}{1 - \sin^2 \theta}$$

$$\frac{\cos \theta - \sin \theta \cos \theta - \cos \theta - \sin \theta \cos \theta}{\cos^2 \theta}$$

$$\frac{-2 \sin \theta \cos \theta}{\cos^2 \theta}$$

$$-2 \tan \theta \quad \checkmark$$

11. $\csc^2 \theta - \sin^2 \theta - \cos^2 \theta - \cot^2 \theta = 0$

$$(\cancel{1 + \cot^2 \theta}) + (\cancel{\cos^2 \theta - 1}) - \cos^2 \theta - \cot^2 \theta = 0$$

$$0 = 0 \quad \checkmark$$

$$12. \sin \theta + \frac{\cos \theta}{\tan \theta} = \csc \theta$$

$$\sin \theta + \frac{\cos \theta}{\frac{\sin \theta}{\cos \theta}}$$

$$\sin \theta + \cos \theta \cdot \frac{\cos \theta}{\sin \theta}$$

$$\sin \theta + \frac{\cos^2 \theta}{\sin \theta}$$

$$\frac{\sin^2 \theta}{\sin \theta} + \frac{\cos^2 \theta}{\sin \theta}$$

$$\frac{1}{\sin \theta}$$

$$\csc \theta \quad \checkmark$$

$$14. \frac{\csc \theta}{\sin \theta} + \frac{\cot \theta}{\cos \theta} = \cot^2 \theta + \csc \theta + 1$$

$$\frac{\csc \theta \cos \theta}{\sin \theta \cos \theta} + \frac{\cot \theta \sin \theta}{\sin \theta \cos \theta}$$

$$\frac{\cot \theta}{\sin \theta \cos \theta} + \frac{\cos \theta}{\sin \theta \cos \theta}$$

$$\frac{\cot \theta}{\sin \theta \cos \theta} + \frac{1}{\sin \theta}$$

$$\frac{\cos \theta}{\sin \theta \cos \theta} + \csc \theta$$

$$\frac{\cos \theta}{\sin \theta} \cdot \frac{1}{\sin \theta \cos \theta} + \csc \theta$$

$$\frac{1}{\sin^2 \theta} + \csc \theta$$

$$\csc^2 \theta + \csc \theta$$

$$(\cot^2 \theta + 1) + \csc \theta$$

$$\cot^2 \theta + \csc \theta + 1 \quad \checkmark$$

$$13. \frac{\cos \theta}{1 + \sin \theta} = \sec \theta - \tan \theta$$

$$\frac{(1 - \sin \theta) \cos \theta}{1 - \sin^2 \theta} =$$

$$\frac{\cos \theta - \sin \theta \cos \theta}{\cos^2 \theta}$$

$$\frac{\cos \theta}{\cos^2 \theta} - \frac{\sin \theta \cos \theta}{\cos^2 \theta}$$

$$\frac{1}{\cos \theta} - \frac{\sin \theta}{\cos \theta}$$

$$\sec \theta - \tan \theta \quad \checkmark$$

$$15. \frac{1 + \sin \theta}{\sin \theta} + \frac{\sin \theta}{1 - \sin \theta} = \frac{\csc \theta}{1 - \sin \theta}$$

$$\frac{1 - \sin^2 \theta}{(1 - \sin \theta) \sin \theta} + \frac{\sin^2 \theta}{(1 - \sin \theta) \sin \theta}$$

$$\frac{1}{(1 - \sin \theta) \sin \theta}$$

$$\frac{1}{(1 - \sin \theta) \sin \theta}$$

$$\frac{1}{1 - \sin \theta} \cdot \frac{1}{\sin \theta}$$

$$\frac{1}{1 - \sin \theta} \cdot \csc \theta$$

$$\frac{\csc \theta}{1 - \sin \theta} \quad \checkmark$$

$$16. 4\sec\theta + 2\sqrt{3} = \sec\theta$$

$$3\sec\theta + 2\sqrt{3} = 0$$

$$3\sec\theta = -2\sqrt{3}$$

$$\sec\theta = \frac{-2\sqrt{3}}{3} = -\frac{2}{\sqrt{3}}$$

$$\cos\theta = -\frac{\sqrt{3}}{2}$$

$$\theta = \frac{5\pi}{6}, \frac{7\pi}{6}$$

$$17. 2\tan\theta + 4 = \tan\theta + 5$$

$$2\tan\theta = \tan\theta + 1$$

~~$$\tan\theta = \tan\theta + 1$$~~

$$\tan\theta = 1$$

$$\theta = \frac{\pi}{4}, \frac{5\pi}{4}$$

$$18. 4\cos^2\theta + 2 = 3$$

$$4\cos^2\theta = 1$$

$$\cos^2\theta = \frac{1}{4}$$

$$\cos\theta = \pm \frac{1}{2}$$

$$\theta = \frac{\pi}{3}, \frac{2\pi}{3}, \frac{4\pi}{3}, \frac{5\pi}{3}$$

$$19. \cos\theta - 1 = \sin\theta$$

$$\cos^2\theta - 2\cos\theta + 1 = \sin^2\theta$$

$$\cos^2\theta - 2\cos\theta + 1 = 1 - \cos^2\theta$$

$$2\cos^2\theta - 2\cos\theta = 0$$

$$2\cos\theta(\cos\theta - 1) = 0$$

$$2\cos\theta = 0 \quad \cos\theta = 1$$

$$\theta = \frac{\pi}{2}, \frac{3\pi}{2} \quad \theta = 0$$

~~20.~~
$$\cos\theta \tan\theta - \sin^2\theta = 0$$

$$\cos\theta \cdot \frac{\sin\theta}{\cos\theta} - \sin^2\theta = 0$$

$$\sin\theta - \sin^2\theta = 0$$

$$\sin\theta(1 - \sin\theta) = 0$$

$$\sin\theta = 0 \quad \sin\theta = 1$$

$$\theta = 0, \pi \quad \theta = \frac{\pi}{2}$$

$$\theta = \pi n, n \in \mathbb{Z}$$

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$$21. 3\sin^2\theta + 6 = 2\sin^2\theta + 7$$

$$\sin^2\theta = 1$$

$$\sin\theta = \pm 1 \quad \theta = 0, \frac{\pi}{2}, \frac{3\pi}{2}, \dots$$

$$\theta = \frac{\pi}{2} + \pi n, n \in \mathbb{Z}$$

$$22. \sin\theta + \cos\theta = 0$$

$$\sin\theta = -\cos\theta$$

$$\theta = \frac{3\pi}{4}, \frac{7\pi}{4}, \dots$$

$$\theta = \frac{3\pi}{4} + \pi n, n \in \mathbb{Z}$$

$$23. \sec\theta + \tan\theta = 0$$

$$\frac{1}{\cos\theta} + \frac{\sin\theta}{\cos\theta} = 0$$

$$\frac{1 + \sin\theta}{\cos\theta} = 0$$

$$1 + \sin\theta = 0$$

$$\sin\theta = -1$$

~~$$\theta = \frac{3\pi}{2}$$~~

no solution

$$24. 3 - 3\cos^2\theta = 1 + \sin^2\theta$$

$$3(1 - \cos^2\theta) = 1 + \sin^2\theta$$

$$3\sin^2\theta = 1 + \sin^2\theta$$

$$2\sin^2\theta = 1$$

$$\sin^2\theta = \frac{1}{2}$$

$$\sin\theta = \pm \frac{1}{\sqrt{2}} = \pm \frac{\sqrt{2}}{2}$$

~~$$\theta = \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$$~~

$$\frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}, \dots$$

$$\theta = \frac{\pi}{4} + \frac{\pi}{2}n, n \in \mathbb{Z}$$

$$25 \quad 185 = \frac{(82)^2 \sin 2\theta}{32}$$

$$5,920 = 6,724 \sin(2\theta)$$

$$\frac{5,920}{6,724} = \sin 2\theta$$

$$\sin^{-1}\left(\frac{5,920}{6,724}\right) = \theta$$

$$\theta = 30.8^\circ, 59.2^\circ$$

$$\begin{aligned} 260. h &= 75 + 70 \sin\left(\frac{\pi}{25} \cdot 0 - \frac{\pi}{2}\right) \\ &= 75 + 70 \sin\left(-\frac{\pi}{2}\right) \\ &= 75 + 70(-1) \\ &= \text{~~45~~ } 5 \text{ ft} \end{aligned}$$

$$0. \quad 145 = 75 + 70 \sin\left(\frac{\pi}{25} t - \frac{\pi}{2}\right)$$

$$70 = 70 \sin\left(\frac{\pi}{25} t - \frac{\pi}{2}\right)$$

$$1 = \sin\left(\frac{\pi}{25} t - \frac{\pi}{2}\right)$$

$$\sin^{-1}(1) = \frac{\pi}{25} t - \frac{\pi}{2}$$

$$\frac{\pi}{2} = \frac{\pi}{25} t - \frac{\pi}{2}$$

$$\pi = \frac{\pi}{25} t$$

$$25 \text{ sec} = t$$